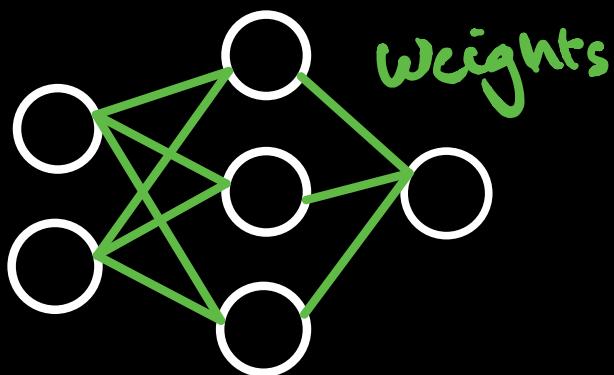


A neural network in plain Numpy

1. initial network



initiate with
small numbers

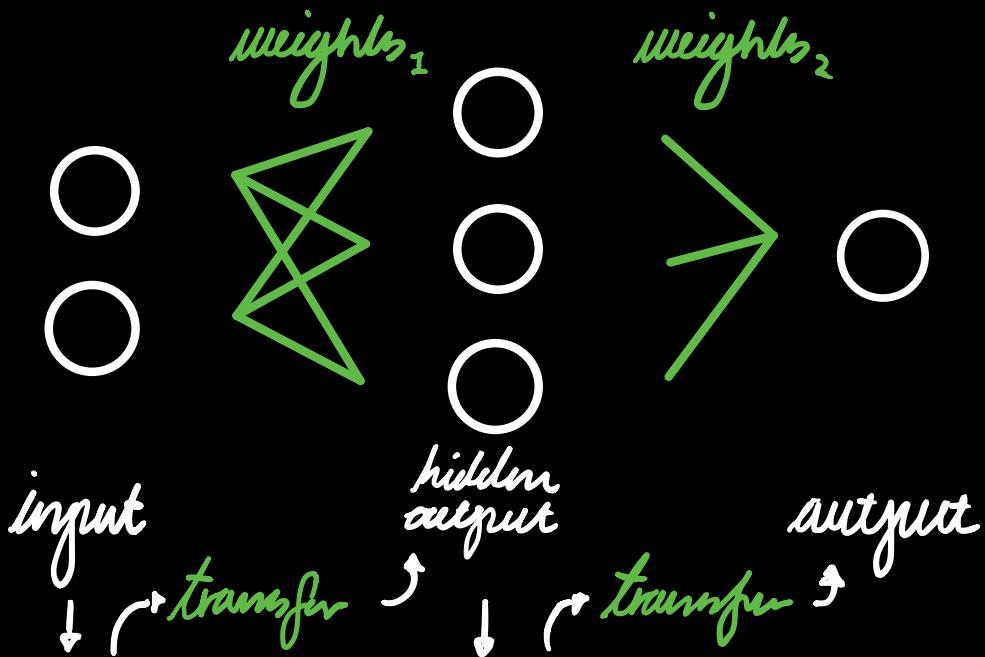
2. the forward propagation

activation → transfer → forward prop

$$\text{activation} : \sum_{i=1}^N w_i \cdot \text{input}_i + \text{bias}$$

$$\text{transfer} : \frac{1}{1 + e^{-\text{activation}}} \quad \begin{array}{c} \text{sigmoid} \\ \text{graph} \end{array}$$

forward prop :



activation activation

3. back propagate error

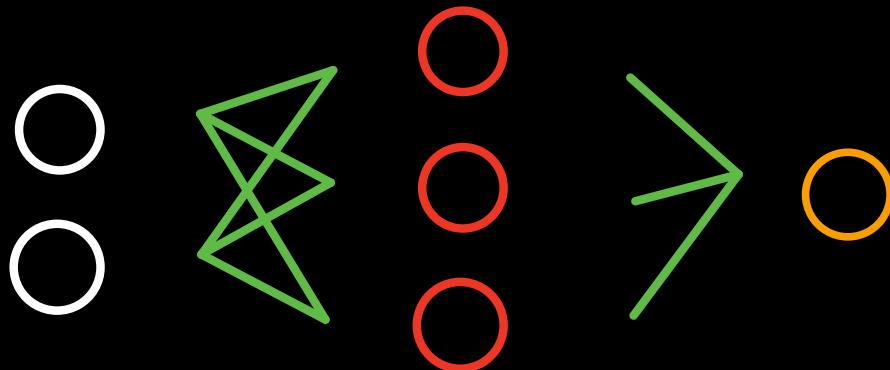
transfer derivative \rightarrow error backprop

transfer derivative: $output \times (1 - output)$
(derivative of sigmoid)

error backprop:

$$\text{error}_{\text{output}} = (\text{expected} - \text{output}) \cdot \text{transfer derivative}$$

where expected is the expected output from each neuron.



$$\text{error}_{\text{HIDDEN}} = (\text{weight}_k \cdot \text{error}_j) \cdot \text{transfer derivative}$$

where error_j is the error from neuron j and weight_k is the weight connecting the k^{th} neuron to the current neuron.

4. train network

update weights \rightarrow train network

update: weight + learning rate · error · input

train:

for epoch in epochs:

$$\text{sum(error)} = 0$$

for row in train:

1. forward prop
2. calculate expected
3. backprop error
4. update weights

5. predict

forward prop \rightarrow argmax

forward: take trained network and forward prop the new input.

argmax: given the new output, choose the highest input with argmax